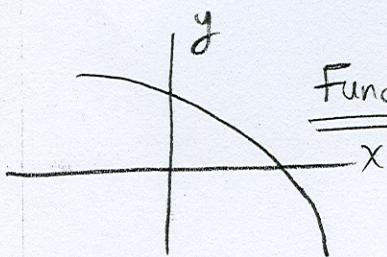


MA103 Final Exam Review Problems
Revised 2006 (Fall)

Page of 29

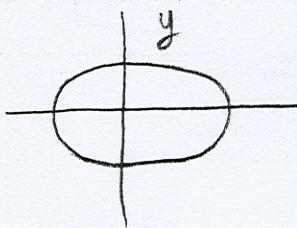
#2)



a)

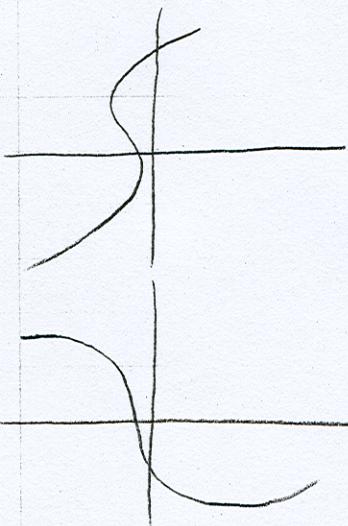
Function; every x has only one y value

b)



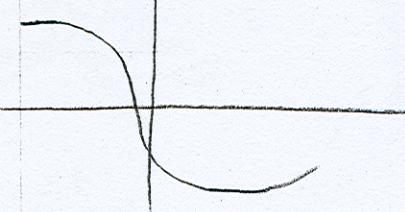
Not a function; B/c one x can have two y values. (This graph fails Vertical Line test)

c)



Not a function; B/c one x can have two y values. (This graph fails V. Line test)

d)



function; B/c every x has only one y value

#3)

$$2x + 3y = 18 \Rightarrow 3y = -2x + 18 \Rightarrow y = -\frac{2}{3}x + 6$$

a)

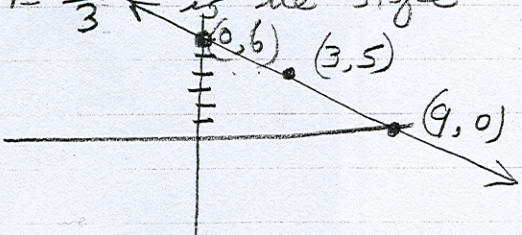
find x intercept; let $y = 0$ $2x = 18 \Rightarrow x = 9$ $\boxed{(9, 0)}$ \leftarrow x int

b)

find y intercept; let $x = 0$ $3y = 18 \Rightarrow y = 6$ $\boxed{(0, 6)}$ \leftarrow y int

c)

find the slope; $m = -\frac{2}{3}$ \leftarrow is the slope



d) sketch the graph

$$y = mx + b$$

$$-2 = -\frac{2}{3}(-3) + b$$

$$-2 = 2 + b$$

$$\boxed{-4 = b}$$

$$\Rightarrow \boxed{y = -\frac{2}{3}x - 4}$$

#4 $f(x) = 4x^2 - 3x - 6$

$$f(x) = 4\left(x^2 - \frac{3}{4}x + \frac{9}{64}\right) - 6 - \frac{9}{16}$$

$$\left(\frac{\frac{3}{4}}{2}\right)^2 = \frac{9}{64}$$

$$f(x) = 4\left(x - \frac{3}{8}\right)^2 - \frac{105}{16}$$

a) $f(x) = a(x-h)^2 + k \quad \left\{ \Rightarrow \text{Vertex} = \left(\frac{3}{8}, -\frac{105}{16}\right)\right.$

b) $x = \frac{-b}{2a} = \frac{-(-3)}{2(4)} = \frac{3}{8} \Rightarrow f\left(\frac{3}{8}\right) = -\frac{105}{16} \Rightarrow \text{Vertex} = \left(\frac{3}{8}, -\frac{105}{16}\right)$

Vertex $\left(\frac{3}{8}, -\frac{105}{16}\right)$ by Graphing the $y_1 = 4x^2 - 3x - 6$

c) $(-0.906, 0), \text{ & } (1.656, 0)$

d) To find y-intercept let $x=0 \Rightarrow (0, -6) = \text{y-intercept}$

#5 a) $\sqrt{48} = \sqrt{16} \sqrt{3} = 4\sqrt{3}$

b) $\frac{5}{\sqrt{15}} = \frac{5}{\sqrt{15}} \cdot \frac{\sqrt{15}}{\sqrt{15}} = \frac{5\sqrt{15}}{15} = \frac{\sqrt{15}}{3}$

c) $3\sqrt{20} - 7\sqrt{45} + \sqrt{5} = 3\sqrt{4\cdot 5} - 7\sqrt{9\cdot 5} + \sqrt{5} = 6\sqrt{5} - 21\sqrt{5} + \sqrt{5} = -14\sqrt{5}$

#6 $f(x) = 3 - 4x$

a) $f(-2) = 3 - 4(-2) = 3 + 8 = 11$

b) $f(x) = -2 \Rightarrow 3 - 4x = -2 \Rightarrow -4x = -5$

$$x = \frac{-5}{-4} = \frac{5}{4}$$

#7) $f(x) = 3x^2 - 6x + 1$

To find x intercept let $y=0 \Rightarrow 3x^2 - 6x + 1 = 0$

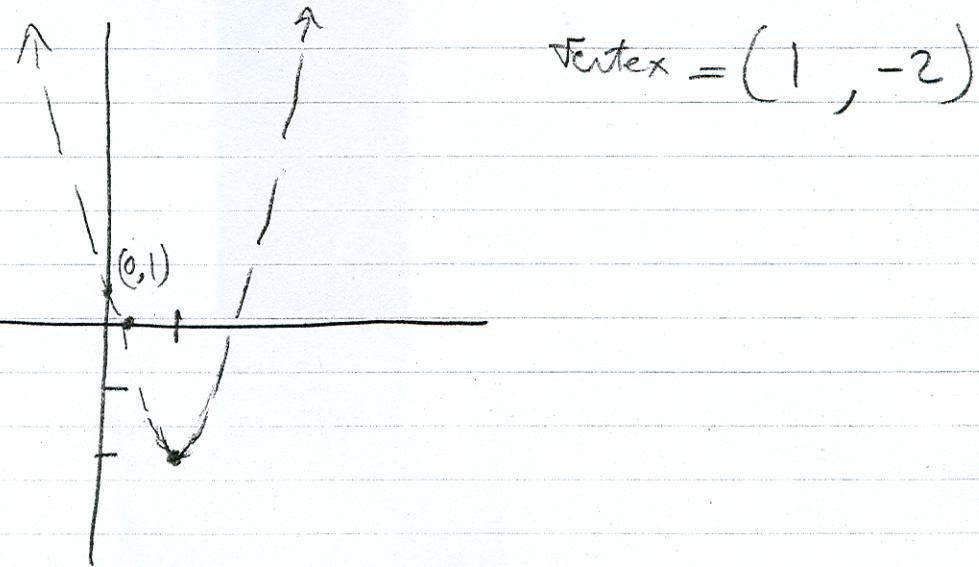
$$\begin{aligned} x &= \frac{6 \pm \sqrt{36 - 12}}{6} = \frac{6 \pm \sqrt{24}}{6} \\ &= \frac{6 \pm 2\sqrt{6}}{6} \Rightarrow (1.816, 0) \\ &\quad \Rightarrow (0.184, 0) \end{aligned}$$

To find y intercept let $x=0 \Rightarrow y$ intercept $(0, 1)$

b) $f(2) = 3(2)^2 - 6(2) + 1 = 1$

$$f(-2) = 3(-2)^2 - 6(-2) + 1 = 25$$

c)



d) $x_{\text{vertex}} = \frac{-b}{2a} = \frac{-(-6)}{2(3)} = \frac{6}{6} = 1$

#7 Continued

$$g(x) = -9x - 2x^2 = -2x^2 - 9x$$

(a) Find all Intercepts

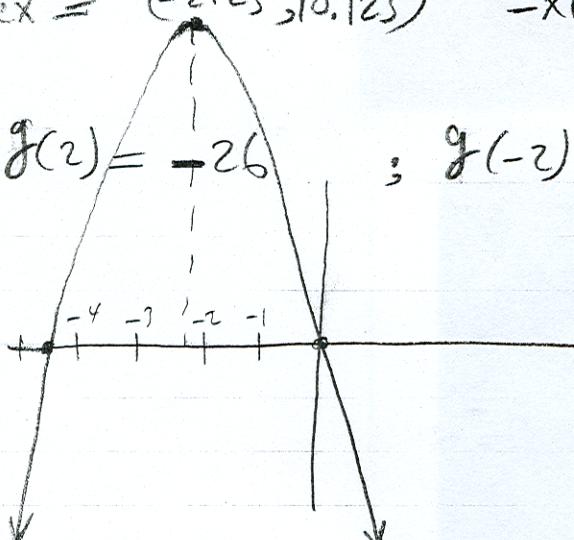
To find y intercept let $x=0 \Rightarrow y=0 \Rightarrow y\text{ intercept } (0,0)$ To find x intercept let $y=0 \Rightarrow -9x - 2x^2 = 0$

$$\text{vertex} = (-2.25, 10.125) \quad -x(9+2x)=0 \Rightarrow (x=0, y=0)$$

OR
 $(x = -\frac{9}{2}, y=0)$

b) $g(2) = -26$; $g(-2) = 10$

c)



d) $x = -\frac{b}{2a} = -\frac{(-9)}{2(-2)} = -\frac{9}{4} = -2.25 \quad y = 10.125$

\times h(x) = $x^3 - 2x - 6$

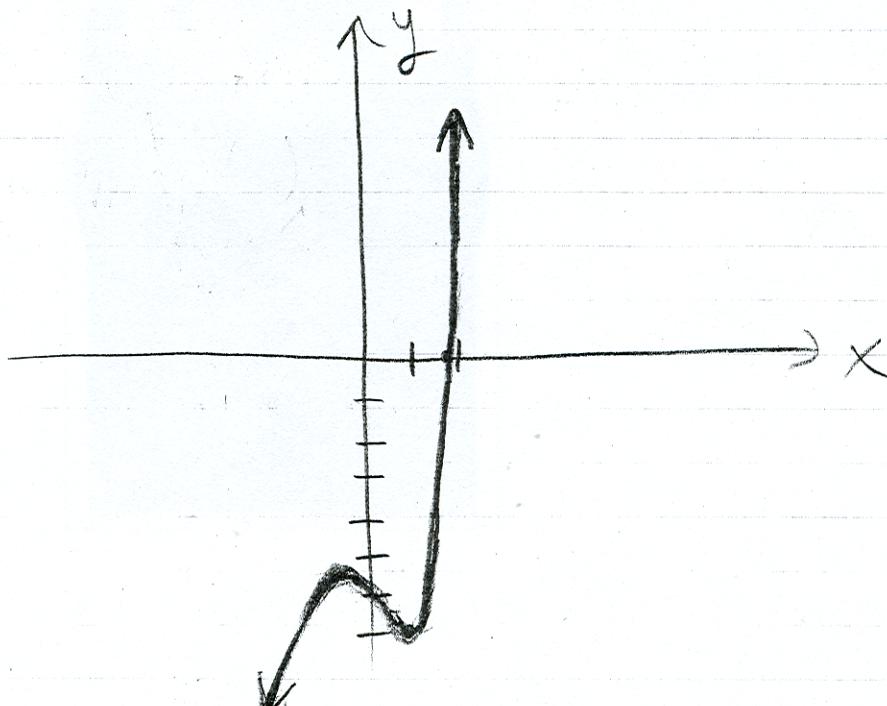
$y\text{ intercept } (0, -6)$

$y\text{ intercept}$ let $x=0 \Rightarrow y=-6$

$x\text{ intercept } (2.18, 0)$

$$h(2) = 0$$

$$h(-2) = -14$$



#8) a) $8x^{\frac{1}{3}} = 8\sqrt[3]{x}$

b) $(-8x)^{\frac{1}{3}} = (-8)^{\frac{1}{3}}(x)^{\frac{1}{3}} = -2\sqrt[3]{x}$

c) $(8x)^{\frac{1}{3}} = \frac{1}{(8x)^{\frac{1}{3}}} = \frac{1}{8^{\frac{1}{3}}x^{\frac{1}{3}}} = \frac{1}{2\sqrt[3]{x}}$

d) $(3x^{\frac{3}{4}})(16x)^{\frac{1}{4}} = 3x^{\frac{3}{4}} \cdot 16^{\frac{1}{4}} x^{\frac{1}{4}}$

$$= 3x^{\frac{3}{4}} \cdot 2^{\frac{1}{4}} x^{\frac{1}{4}} = 6x^{\frac{4}{4}} = 6x$$

e) $\frac{x^{\frac{1}{2}}}{x^{\frac{5}{2}}} = x^{\frac{1}{2} - \frac{5}{2}} = x^{-\frac{4}{2}} = x^{-2} = \frac{1}{x^2}$

#9) $\frac{8 - \sqrt{-36}}{4} = \frac{8 - 6i}{4} = \frac{8}{4} - \frac{6}{4}i$

$$= \boxed{2 - \frac{3}{2}i}$$

$$\text{#10) } \text{a) } \sqrt{x} \cdot \sqrt[3]{x} = x^{\frac{1}{2}} \cdot x^{\frac{1}{3}} = x^{\frac{3+2}{6}}$$

$$= x^{\frac{5}{6}}$$

$$\text{b) } 5\sqrt{3} - \sqrt{3} = 4\sqrt{3}$$

#9] Simplify $\frac{8-\sqrt{-36}}{4} = \frac{8-6i}{4} = \frac{8}{4} - \frac{6i}{4} = 2 - \frac{3}{2}i$

#11) a) $(x+3)^2 - 81 = 0$ b) $3x^2 + 5x = 2$
 $(x+3)^2 = 81$ $3x^2 + 5x - 2 = 0$
 $(x+3) = \pm 9$ $(3x-1)(x+2) = 0$
 $x+3 = 9$ $3x-1 = 0$ $x+2 = 0$
 $x = 9-3 = 6$ $x = -\frac{1}{3}$ $x = -2$

c) $(x+1)(x-2) = 18$ d) $2x^2 - 4x + 5 = 0$
 $x^2 - 2x + x - 2 = 18$ Will Not factor; So, use Quad formula
 $x^2 - x - 20 = 0$
 $(x-5)(x+4) = 0$
 $x = 5$ $x = -4$
 $x = \frac{-(-4) \pm \sqrt{(-4)^2 - 4(2)(5)}}{2(2)}$
 $x = \frac{4 \pm \sqrt{-24}}{4} = \frac{4 \pm 2\sqrt{6}i}{4}$
 $x = 1 \pm \frac{1}{2}\sqrt{6}i$

Extra) $x(x^2 + 3x - 1) = 3$ $\rightarrow (x+3)(x+1)(x-1) = 0$
 $x^3 + 3x^2 - x = 3$
 $x^3 + 3x^2 - x - 3 = 0$
 $x^2(x+3) - 1(x+3) = 0$
 $(x+3)(x^2 - 1) = 0$

#13

$$X = 1.1578074156$$

↓ ↓ ↓ ↓ ↓
tenths hundredths thousandths ten thousandths hundred thousandths

$$Y = 2E - 13$$

↑

-13

this means $Y = 2 \times 10^{-13}$
which is almost zero

So, the coordinates of x-intercept is:

$$(1.158, 0)$$

#12

$$f(t) = -0.19t^2 + 2.56t - 2.37$$

Where $f(t)$ represents the amount of profit in millions of \$
 t is the number of years since 1995

a) Year 2003

$$t = 2003 - 1995 = 8$$

$$f(8) = -0.19(8)^2 + 2.56(8) - 2.37 = 5.95$$

So the profit in 2003 was \$5.95 million.

b) $f(t) = 4.23 = -0.19t^2 + 2.56t - 2.37$

Now; Solve by Graphing or Quad formula $\Rightarrow t = 3.47 \& t = 10$

So, In the years $1995 + 3 = 1998$ and $1995 + 10 = 2005$,
the profit was \$ 4.23 million

c) When t is negative the Company didn't exist.

Also the model predicts losses after 2008.

d) $f(t) = 0 ; t = 1 \& t = 12.47 \approx 12.5 \approx 13$

In the years 1996 & 2008, the profit is 0.

e) Vertex $t = \frac{-b}{2a} = \frac{-2.56}{2(-0.19)} = 6.73$ the Company will have
Max profit in the year 2002

#14) Solve for x

$$\frac{x}{x+1} + \frac{2x-2}{x} = -\frac{1}{x+1}$$

Step I) find LCD and multiply every term by that LCD

$$\cancel{x(x+1)} \frac{x}{\cancel{x+1}} + \frac{(2x-2)x(x+1)}{\cancel{x}} = -\frac{1 \times (x+1)}{\cancel{x+1}}$$

$$x^2 + (2x-2)(x+1) = -x$$

Step II) Simplify & solve for x .

$$x^2 + 2x^2 + 2x - 2x - 2 = -x$$

$$3x^2 - 2 + x = 0$$

$$3x^2 + x - 2 = 0$$

Now solve by factoring or quad formula.

$$(3x - 2)(x + 1) = 0$$

$$3x - 2 = 0 \quad x + 1 = 0$$

$$x = \frac{2}{3}$$

$$x = -1$$

But $x = -1$ is called extraneous solution (ie No Good soln.)So, the final answer is $x = \frac{2}{3}$

$$\#14 \text{ Continued} \quad 2x+1 = \sqrt{7-x}$$

We will square both sides to solve for x

$$(2x+1)^2 = (\sqrt{7-x})^2$$

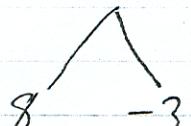
$$(2x+1)(2x+1) = 7-x$$

$$4x^2 + 4x + 1 = 7 - x$$

$$+x -7 -7+x$$

$$4x^2 + 5x - 6 = 0$$

Now solve by factoring if possible; $(4)(-6) = -24$



$$4x^2 + 8x - 3x - 6 = 0$$

$$4x(x+2) - 3(x+2) = 0$$

$$(x+2)(4x-3) = 0$$

$$x = -2 \quad \text{or} \quad x = \frac{3}{4}$$

But $x = -2$ is called extraneous sln because:

$$2(-2)+1 \neq \sqrt{7-(-2)}$$

So, the only Answer is $\boxed{\underline{\underline{x = \frac{3}{4}}}}$