

NAME Solutions SCORE: _____/20
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Let the demand and supply functions be represented by $D(p)$ and $S(p)$, where p is the price in dollars.

$$D(p) = 4000 - 35p \qquad S(p) = 95p$$

- A. Find the price when the demand is 2700. Is there a surplus or a shortage at this price? (3 Points)

Using $D(p)$, $2700 = 4000 - 35p$

$-1300 = -35p \rightarrow p = -1300/-35 = 37.14 \rightarrow \text{price} = \37.14

$S(p) = S(37.14) = 95(37.14) = 3528.3$

$S = 3528.3 > D = 2700$ when the price, $p = \$37.14$ so there is a surplus.

**In general, you must support surplus with the statement $S > D$ and shortage with the statement $S < D$.

- B. Find the equilibrium price and demand (supply) for the given functions. (3 Points)

Solve $D = S$ $4000 - 35p = 95p$

$4000 = 130p$ $P = 4000/130 = 30.77$; therefore $p = \$30.77$

and $S(30.77) = 95*30.77 = 2923.15$

Then, the **equilibrium price and demand (supply) = (\$30.77 , 2923.15)**

- C. At what prices is there a surplus? (3 Points)

For prices $p > \$30.77$

- D. At what prices is there a shortage? (3 Points)

For prices $p < \$30.77$

** In general, for the Supply/Demand problems that are covered in this course, surplus is when $p >$ equilibrium price and shortage is when $p <$ equilibrium price.

$$(x_1, y_1)$$

$$(x_2, y_2)$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$y = mx + b$$

$$y - y_1 = m(x - x_1)$$

2) Write the equation of the line through $(-15, -3)$ with

$$\text{slope } m = \frac{3}{5}$$

(4 Points)

Method 1: You can use the point-slope formula as follows:

$$y - y_1 = m(x - x_1)$$

$$y - (-3) = \frac{3}{5}(x - (-15))$$

$$y + 3 = \frac{3}{5}x + 9$$

$$y = \frac{3}{5}x + 9 - 3$$

$$y = \frac{3}{5}x + 6$$

Method 2: Use the slope-intercept form as follows:

$$y = mx + b$$

$$-3 = \frac{3}{5}(-15) + b$$

$$-3 = -9 + b$$

$$-3 + 9 = -9 + b + 9$$

$$6 = b$$

$$y = \frac{3}{5}x + 6$$

3) Write the equation of the line through $(-6, 2)$ and $(-7, 5)$

(4 Points)

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{5 - 2}{-7 - (-6)} = -3$$

$$y - 2 = -3(x - (-6))$$

$$y - 2 = -3x - 18$$

$$y = -3x - 16$$