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1) A company manufactures skate boards.

$C(x) = 80x + 200$ represents the cost for a company that manufactures skateboards, where x is the number of skateboards manufactured and C is the cost, in dollars, of making x skateboards.

A. Interpret the slope of the equation in the context of the problem.

For each additional skateboard manufactured the cost increases by \$80.

B. How much will it cost the company to produce 50 skateboards per day?

$$C = 80(50) + 200 = 4000 + 200 = \$4200$$

C. If the company has enough investments to spend \$3000 per day on production, how many skateboards can be made daily?

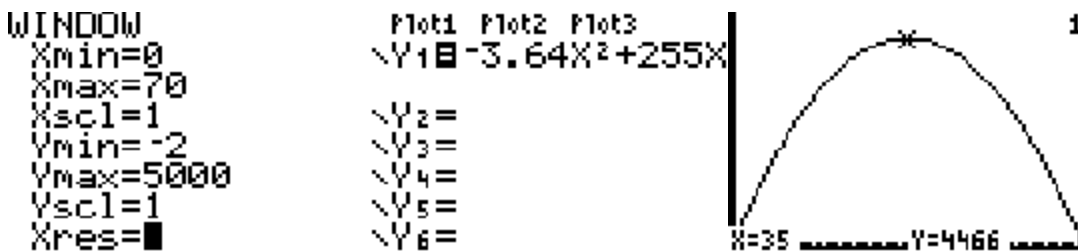
$$3000 = 80x + 200 \rightarrow 2800 = 80x \rightarrow x = 2800/80 = 35 \text{ Skateboards}$$

OVER →→→→→

- 2) The Polaroid company manufactures a new product The PoGo – a pocket size photo printer. The following functions have been established for this product:
 Revenue: $R(x) = -3.64x^2 + 255x$ and Cost: $C(x) = 1800 + 40x$
 where x , $0 \leq x \leq 70$, is in hundreds, and $R(x)$ and $C(x)$ are in hundreds of dollars.
- A. What is the production level of PoGos (to the nearest hundred) at which the company would reach its maximum revenue level.

Using the revenue equation: $R(x) = -3.64x^2 + 255x$, I applied the $x = -b/2a$ formula for finding the x-coordinate of the vertex (that is where the maximum revenue will occur). $a = -3.64$ and $b = 255$, so $x = -b/2a = -255/(2*-3.64) = 35$, 35 hundred PoGo

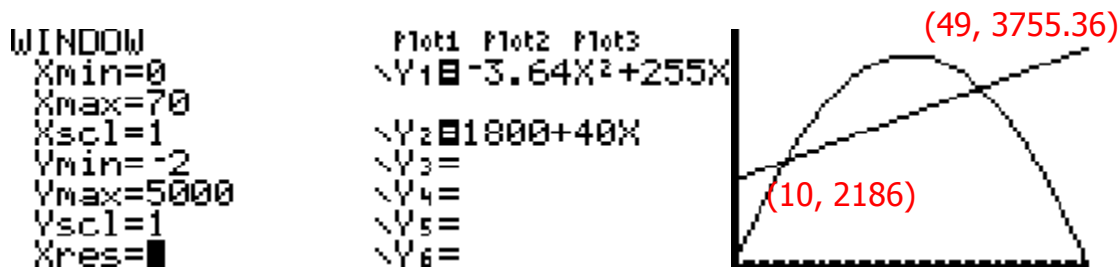
If I want to find this value using a graph, I need to determine the y_{\max} for my window. $x_{\min} = 0$ and $x_{\max} = 70$ (these are given by $0 \leq x \leq 70$ from above), the $y_{\min} = 0$. To find a reasonable y_{\max} , pick a value of x between 0 & 70. I will use $x = 35$, for $R(x) = -3.64x^2 + 255x$, $R(35) = -3.64(35)^2 + 255(35) = 4466$. I will use $y_{\max} = 5000$



If using calculator, state window size and answer $x = 35$ hundred PoGos.

Either way the result is: The company must produce 3,500 PoGos to achieve its maximum revenue.

- B. Find the production level(s) of PoGos (to the nearest hundred) at which the company has break-even point(s). Sketch a simple graph and indicate your answers on the graph.



Use 5:intersect to find the values. State your window settings, sketch a graph (like above) and state: The company must produce 1000 or 4,900 PoGos to break-even.

- C. Will the company make a profit or a loss if it manufactures and sells 1500 PoGos? Explain.

They will make a profit since 1,500 (15 hundred) is in between the break-even production levels of 1,000 and 4,900. The revenue for 15 hundred PoGos is greater than the cost.