## MATH 120 Section 4.1 Systems of Linear Equations in Two Variables

A system of linear equations consists of two or more linear equations, which are solved simultaneously.
A solution to a system consists of the values of the variables which make the system true.

## Three Methods for Solving Systems

I. Graphing
II. Substitution

Solve one equation for a variable and substitute into the other equation.
III. Elimination (Sometimes called Addition)

- Multiply one or both equations by a value or values, so that the coefficients of one variable in both equations are the same number but opposite signs.
- Add the equations so that one variable is eliminated.


## Problems

1. Solve the system of linear equations by the following methods:
a) Graphing, b) Elimination, c) Substitution.

$$
\left\{\begin{array}{l}
2 x+y=8 \\
x+3 y=9
\end{array}\right.
$$


2. Animals in an experiment are to be kept under a strict diet. Each animal should receive 60 grams of protein and 10 grams of fat. The laboratory technician is able to purchase two food mixes: Mix A has 20\% protein and 6\% fat. Mix B has 50\% protein and $5 \%$ fat. Complete the chart. Write and solve a system of equations to determine how many grams of each mix should be used to obtain the right diet for one animal?

|  | Grams of Mix A | Grams of Mix B | Total |
| :--- | :--- | :--- | :--- |
| Protein |  |  |  |
| Fat |  |  |  |

4. A company produces lawn mowers. The company's daily fixed costs are $\$ 42,000$ and variable costs are $\$ 1500$ per lawn mower. The mowers are sold for $\$ 1800$ each.
a) Find the cost function $C(x)$.
b) Find the revenue function $R(x)$.
c) Find the break-even point. Write your answer as an ordered pair.

d) Graph the cost and revenue functions on the given coordinate system and show the break-even point.
e) Write the meaning of the break-even point you found in part $c$ using complete sentences with correct units. Include an interpretation of the regions between the lines that are to the left and to the right of the breakeven point.
5. A company markets exercise DVDs that sell for $\$ 34.95$, including shipping and handling. The monthly fixed costs (advertising, rent, etc.) are \$47,700 and the variable costs (materials, shipping, etc.) are $\$ 12.45$ per DVD.
a) Find the cost function $C(x)$.
b) Find the revenue function $R(x)$.
c) Find the break-even point. Write your answer as an ordered pair.
d) Graph the cost and revenue functions on the given coordinate system and show the break-even point.
e) Write the meaning of the break-even point
 you found in part c using complete sentences with correct units. Include an interpretation of the regions between the lines that are to the left and to the right of the break-even point.
