Name $\qquad$

1. A factory has two machines that produce bolts. Machine I produces $60 \%$ of the bolts, and $3 \%$ of its bolts are defective. Machine II produces $40 \%$ of the bolts and $2 \%$ of its bolts are defective.
A. Draw a probability tree for the given information.

B. If it is given that a bolt came from Machine I, what is the probability that it is defective? $\quad P(D \mid I)$
$P(D \mid I)=0.03$
C. What is the probability that a bolt selected at random came from Machine II and is defective? $P(I I \cap D)$
$\mathrm{P}(\mathrm{II} \cap \mathrm{D})=.4(.02)=0.008$
D. What is the probability that a random bolt is defective? $P(D)$
$P(D)=.4(.02)+.6(.03)=.008+.018=.026$
E. Given that a bolt is defective, what is the probability that it came from Machine II? $\quad \mathrm{P}(\mathrm{II} \mid \mathrm{D})$
$\mathrm{P}(\mathrm{II} \mid \mathrm{D})=\frac{.008}{.026}=.307$
