

1. Flu is spreading through a small school. At time  $t$  days after the beginning of the epidemic, there are  $N(t)$  students sick, where  $N(t) = 20t - t^2$ . What is the average rate of change of the number of sick students from  $t = 2$  to  $t = 5$ ? Interpret your answer in a sentence, using appropriate units.

2. The function  $f$  is defined by the graph shown. Based on this graph,

(a)  $\lim_{x \rightarrow -1^-} f(x) =$

(b)  $\lim_{x \rightarrow -1^+} f(x) =$

(c)  $\lim_{x \rightarrow -1} f(x) =$

(d)  $f(-1) =$

- (e) Is  $f$  continuous at  $x = -1$ ? Why or why not? Use limits in your answer.

(f)  $\lim_{x \rightarrow 3^-} f(x) =$

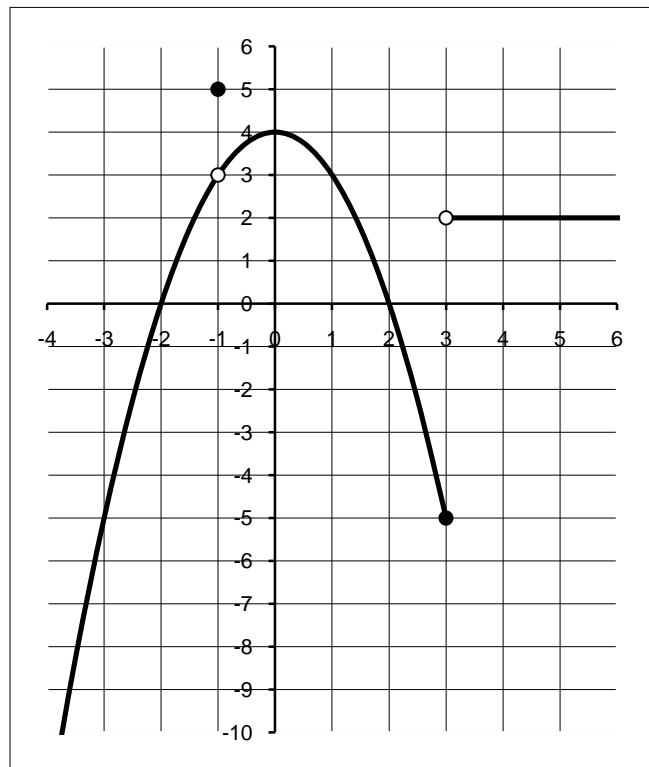
(g)  $\lim_{x \rightarrow 3^+} f(x) =$

(h)  $\lim_{x \rightarrow 3} f(x) =$

(i)  $f(3) =$

- (j) Is  $f$  continuous at  $x = 3$ ? Why or why not? Use limits in your answer.

- (k) Is  $f$  continuous at  $x = 2$ ? Why or why not? Use limits in your answer.



3. Find each limit algebraically. If the limit does not exist, state this.

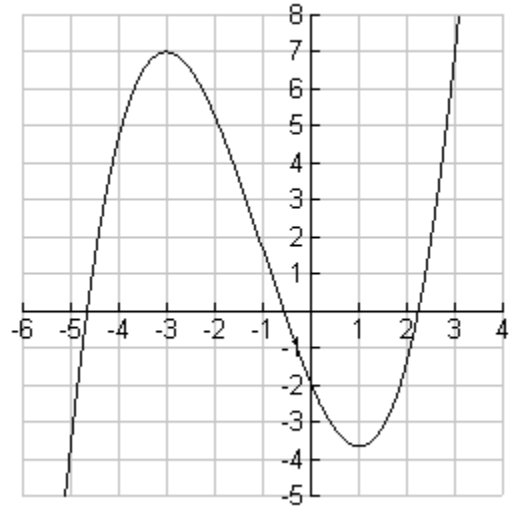
(a)  $\lim_{x \rightarrow 3} \frac{5}{x}$

(b)  $\lim_{x \rightarrow 2} \frac{x}{x-2}$

(c)  $\lim_{x \rightarrow 3} \frac{x^2 + 5x - 24}{x^2 + x - 12}$

4. The graph of a function  $f(x)$  is shown. Based on this graph, for each value of  $x$  given, state whether  $f'(x)$  is positive, negative, or zero.

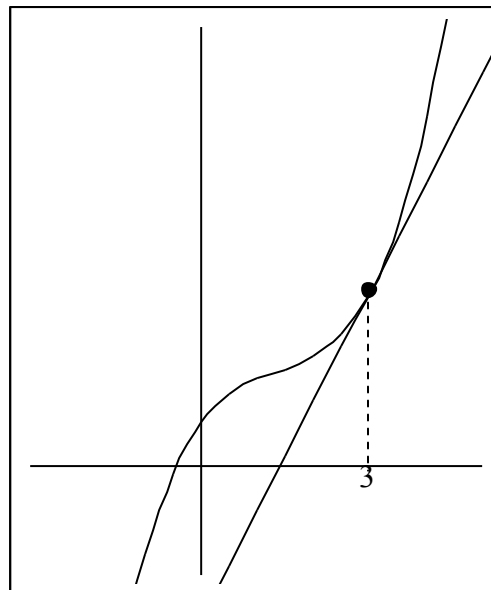
$x$	Is $f'(x)$ zero, negative or positive?
-4	
0	
1	



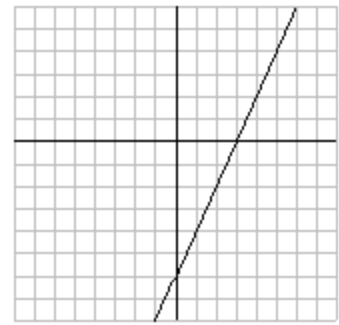
5. The graph of a function  $f(x)$  and its tangent line at  $x = 3$  are shown. The equation of the tangent line is  $y = 10x - 14$ . Based on this graph, determine the value of

(a)  $f(3)$

(b)  $f'(3)$



Graph of  $f'(x)$



9. The graph of  $f'(x)$ , the derivative of a function  $f$  is shown.
- On what intervals is the function  $f$  increasing?
  - On what intervals is the function  $f$  decreasing?
  - At what value of  $x$ , if any, does  $f$  have a local minimum?
  - At what value of  $x$ , if any, does  $f$  have a local maximum?
  - If it is also known that  $f(0) = 0$ , sketch a possible graph of  $f$ .

10. Suppose it is known that  $f'(x) > 0$  for all  $x$  and  $f''(x) < 0$  for all  $x$ . Which of the following could be the graph of  $f(x)$ ?

