

**Name:** \_\_\_\_\_ **Total Possible Points = 150 plus 10 pts extra credit**

1) If  $(5, 2a)$  is a point on the graph of  $3x - 2y = 17$ , what is  $a$ ? (5 Points)

2) Find the  $x$  and  $y$  intercepts of the following  $5x^2 + 6x - 8 - y = 0$  (5 Points)

3) An open box with a square base is required to have a volume of 40 cubic feet. Express the amount  $A$  of material used to make such a box as a function of the length  $x$  of a side of the base. (7 Points)

**Solve**

**4)**

$$\frac{2}{3} - \frac{9}{7x} = \frac{7}{3x}$$

(5 points)

5) City B is located at 75 miles west and 25 miles north of city A. City C is located at 100 miles east and 125 miles south of city A. Find the distance between city B and city C. You can choose city A as the origin of the rectangular coordinate system. Write your answer rounded to two decimal places, if necessary. (5 Points)

6) Find the standard form of equation of a circle with endpoints of a diameter at (5, 9) and (-3, -3) (5 Points)

7) Find the center and radius of the circle with the given equation  $3x^2 + 3y^2 - 24x + 36y - 21 = 0$  (7 points)

8) Find the average rate of change for the function  $f(x) = 4x^3 - 5x + 2$  between -4 to X (7 points)

Algebraically Solve:

9)    $\sqrt{2x+3} - x + 3 = 3$

(6 points)

10) David has 800 yards of fencing and wishes to enclose a rectangular area.

(5 points Each)

a) Express the area  $A$  of the rectangle as a function of the width  $x$  of the rectangle.

b) What is the domain of  $A$ ?

11) Each month a gas station sells  $x$  gallons of gas at \$2.72 per gallon. The cost to the owner of the gas station for each gallon of gas is \$1.99, and the monthly fixed cost for running the gas station is \$37000.

(10 points)

a) Find the cost function. (Hint: Cost = Variable Cost + Fixed Cost)

b) Find the revenue function. (Hint: Revenue = Price \* Quantity)

c) Write an equation that relates the monthly profit, in dollars, to the number of gallons of gasoline sold. (Hint: Profit = Revenue - Cost)

d) If the monthly profit is \$113000, find the number of gallons of gas that are sold in that month.

12) A wire of length  $10X$  is bent into the shape of a circle.

(10 points)

a) Express the circumference of the circle as a function of  $x$ .

▮▮▮ Express the area of the circle as a function of  $x$ .

13) Write an equation of the line passing through the point  $(-6, 5)$  and perpendicular to the line  $y = -3x - 5$ . (10 points)

14) Use long division method and perform  $3x^3 + 2x^2 - x + 3$  divided by  $x - 3$  (10 points)

15) Use Quadratic formula to solve the following:  $4x^2 + 12x = -2$  (6 points)

16) Find the value of  $\frac{f(x+h) - f(x)}{h}$  assuming  $h$  is not zero for the function  $f(x) = 2x^2 - x$   
(Clearly state each of the steps of the process.)

(10 points)

17) Given  $f(x) = -4x^2 + 3x + 2$  Find  $x$  such that  $f(x) = 2$  (5 points)

18) Give the domain of the function. (10 points)

a)  $f(x) = 3x^2 + \frac{2}{x-5} + 5$

b)  $f(x) = \sqrt{-2x+10}$

c)  $f(x) = \frac{x+7}{x^2+13x+42}$

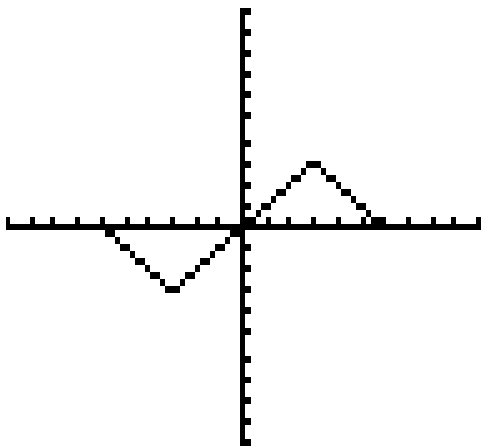
d)  $f(x) = \frac{5x}{\sqrt{-2x+10}}$

19) Let  $P = (x, y)$  be a point on the graph of  $y = x^2 - 1$  (10 points)

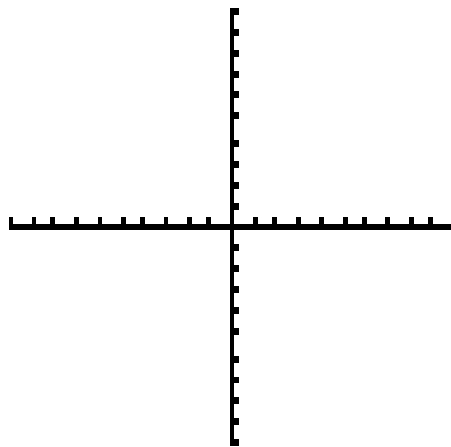
a) Express the distance  $d$  from  $P$  to the origin as a function of  $x$ .

- b) What is  $d$  if  $x = 0$ ?
- c) What is  $d$  if  $x = 1$ ?
- d) For what values of  $x$  is  $d$  smallest?

20) The graph of  $y = f(x)$  is given below;  
(7 points)



Sketch a graph of  $y = -[f(x-3) + 2]$



21) **Extra Credit (10 points)**

Two cars are approaching an intersection. One is 2 miles south of the intersection and is moving at a constant speed of 20 miles per hour. At the same time, the other car is 3 miles east of the intersection and is moving at a constant speed of 30 miles per hour.

- a) Express the distance  $d$  between the cars as a function of time  $t$ .
- b) At time  $t = 1$  hour, what is the distance between the cars?