## Professor Fred Katiraie Calculus I; Quiz Six Version A

Name: $\qquad$

1. Find all value(s) of c (if any) that satisfy the conclusion of the Mean Value Theorem for the function $f(x)=\frac{1}{1+x}$ on the interval $[0,1]$
(3 points)
2. Given that the function $f(x)=x^{3}+a x^{2}+b x$ has critical numbers at $x=1$, and $x=-2$, find $a$ and $b$.
3. Find the minimum value of the function $f(x)=x \ln x$ (Must Justify Your Answer)
4. Find all the points of inflection of $f(x)=x^{5} e^{-x}$
(3 points) (Must Justify Your Answer)
5. Find the Critical numbers of the function $f(x)=x^{\frac{2}{3}}(x-3)^{2}$
(3 points)
6. A farmer has 20 feet of fence, and he wishes to make from it a rectangular pen for his pig Wilbur, using a barn as one of the sides. In square feet, what is the maximum area possible for this pen?
