Professor KatiraieCalculus I Spring 2006;Test IName:Total Possible Points = 140

(24 Points, Domain of each problem is worth 3 Points, and Range is worth 3 Points)

1) Find the **Domain** and **Range** of the following functions:

a)
$$f(x) = \sqrt{(4-3x^2)}$$

b) $g(x) = \ln(\ln(x+5))$

c)
$$g(x) = 1 + \frac{1}{\sin x}$$
 d) $g(x) = 1 + \frac{1}{x}$

(10 Points)

- 2) The graph of g is given.
- a) State the value of g(2)
- b) Is g one-to-one?
- c) Estimate the value of $g^{-1}(3)$?
- d) Estimate the domain of $g^{-1}(x)$
- e) Sketch the graph of $g^{-1}(x)$

(10 Points) 3) Sketch the graph of the following function:

$$f(x) = \begin{cases} 2x+1 & \text{if } x < 2 \\ e^x & \text{if } x \ge 2 \end{cases}$$

(12 Points) 4) Determine whether f is even, odd, or neither even nor odd; (Must Use Definition of Even, Odd Functions)

a)
$$f(x) = 2x^5 - 3x^3 + 2$$

b)
$$f(x) = e^{-x^2}$$

c)
$$f(x) = x + \sin(x)$$

d)
$$f(x) = x^4 + 2x^2 + x$$

(10 Points) 5) A small-appliance manufacturer finds that it costs \$9000 to produce 1000 toaster ovens a week and \$12000 to produce 1500 toaster ovens a week.

a) Express the cost as a function of the number of the toaster ovens produced, assuming that it is linear.

- b) What is the slope of the graph and what does it represent?
- c) What is the y-intercept of the graph and what does it represent?

(5 Points) 6) If $f(x) = 5x + \log(x+10)$, find $f^{-1}(1)$ (10 Points)

7a) Sketch the curve represented by the parametric equation

 $x = \sqrt{t}, \quad y = 1 - t, \quad 0 \le t \le 5$

Indicate with an arrow the direction in which the curve is traced as t increases. Make a table of points with the corresponding values of t.

7b) Eliminate the parameter to find a Cartesian equation of the curve. (Indicate the Domain and Range of the Cartesian equation)

(12 Points)

8) Use the following table to evaluate the expressions.

Х	1	2	3	4	5	6
f(x)	6	5	4	1	3	5
g(x)	6	3	5	1	2	3

- a) f (g(2)) =
- b) g (g(6)) =
- c) (gogof)(5) =
- d) (fogof)(6) =

- (12 Points) 9) Let f be a one-to-one function whose inverse function is given by the formula: $f^{-1}(x) = x^5 - 3x^3 + 5x + 2$
 - a) Compute $f^{-1}(-1)$
 - b) Compute f(1)
 - c) Compute the value of x such that f(x) = 1
 - d) Compute the value of y such that $f^{-1}(y)=1$

(12 Points) 10) Find a formula that describes the following function:

(12 Points) 11) If
$$f(x) = 2x^2 - 3x + 1$$
, find and simplify $\frac{f(x+h) - f(x)}{h}$, $h \neq 0$

(24 Points)

12) Given $f(x) = \ln(x)$ and $g(x) = x^2 - 9$, Find the following and State their Domains:

- a) fog(x)
- b) gof(x)
- c) fof(x)
- d) gog(x)

Extra Credits:

(6 points)

13) Find an expression for the function whose graph consists of the line segment from the point (-2,2) to the point (-1,0) together with the top half of the circle with the center at the origin and radius 1.

Extra Credits:

(4 points)

14) Express the function
$$F(x) = \frac{1}{\sqrt{x + \sqrt{x}}}$$

as a composition of three functions (namely (fogoh)(x)).

(Hint: Find f(x), g(x), and h(x) so that (fogoh)(x) = $\frac{1}{\sqrt{x + \sqrt{x}}}$)